

**Uppgift 1.** a)

$$\begin{aligned}P_1 &= U_F I_1 \cos \varphi \\I_1 &= \frac{1000}{230 \cdot 0.80} = 5.43 A \\ \varphi_1 &= \cos^{-1}(0.80) = 37^\circ \\ \bar{I}_1 &= 5.43 e^{-j37^\circ} A \\ I_2 &= \frac{75 \cdot 10}{230 \cdot 1.0} = 3.26 A \\ \bar{I}_2 &= 3.26 e^{-j120^\circ} A \\ I_3 &= \frac{1500}{230 \cdot 1.0} = 6.52 A \\ \bar{I}_3 &= 6.52 e^{-j240^\circ} A \\ \bar{I}_N &= \bar{I}_1 + \bar{I}_2 + \bar{I}_3 = 0.7 e^{-j141^\circ} A\end{aligned}$$

b)

$$\begin{aligned}P &= P_I + P_{II} = 1870 W \\ Q &= \sqrt{3}(P_{II} - P_I) = 1420.3 VAr\end{aligned}$$

Fullständig faskompensering ger  $Q_{tot} = 0$ .

$$\begin{aligned}Q_C &= -Q \\ Q_C &= -6\pi \cdot 50 \cdot C \cdot 230^2 = -1420.3 \Rightarrow \\ C &= 28.5 \mu F\end{aligned}$$

**Uppgift 2.** a)

$$I_{2M} = \frac{S_M}{\sqrt{3}U_{2M}} = 1804 A$$

b)

$$\begin{aligned}P_{FKM} &= 3R_{2k}I_{2M}^2 \Rightarrow R_{2k} = \frac{P_{FKM}}{3I_{2M}^2} = \frac{9190}{3 \cdot 1804^2} = 0.94 m\Omega \\ U_{2k} &= U_{1k} \frac{U_{2M}}{U_{1M}} = 570 \cdot \frac{400}{10000} = 22.8 V \\ Z_{2k} &= \frac{U_{2k}}{\sqrt{3}I_{2k}} = /I_{2k} = I_{2M}/ = \frac{22.8}{\sqrt{3} \cdot 1804} = 7.3 m\Omega \\ X_{2k} &= \sqrt{Z_{2k}^2 - R_{2k}^2} = \sqrt{0.0073^2 - 0.00094^2} = 7.2 m\Omega\end{aligned}$$

c)

$$\begin{aligned}\cos \varphi &= 0.8 \Rightarrow \sin \varphi = 0.6 \\ \frac{U_2}{\sqrt{3}} &= \frac{U_{20}}{\sqrt{3}} - I_2(R_{2k} \cos \varphi + X_{2k} \sin \varphi) \Rightarrow \\ U_2 &= 400 - \sqrt{3} \cdot 1804 \cdot (0.00094 \cdot 0.8 + 0.0072 \cdot 0.6) = 389.9 V\end{aligned}$$

d)

$$\begin{aligned}P_{ut} &= \sqrt{3}U_H I_L \cos \varphi = \sqrt{3} \cdot 389.9 \cdot 1804 \cdot 0.8 = 974.6kW \\P_{in} &= P_{ut} + P_{F0} + P_{FKM} = 974.6 + 1.5 + 9.2 = 985.3kW \\ \eta &= \frac{P_{in}}{P_{ut}} = 98.9\%\end{aligned}$$

e) Se labb-PM.

**Uppgift 3.** a) Se boken. Pådraget påverkar endast ankarkretsen, dvs inte magnetiseringskretsen.

b) Magnetiseringsströmmen oberoende av ankarströmmen

$$I_m = \frac{220}{400} = 0.55A$$

Vi start är  $E = 0V$

$$U - R_a I_a - E = 0 \Rightarrow I_a = 220/2 = 110A$$

Totala strömmen till motorn

$$I = I_m + I_a = 110.55A$$

c) Vid märkbelatsning:

$$\begin{aligned}I_{a,M} &= I_M - I_m = 9.55 - 0.55 = 9.0A \\ I_{a,start} &= I_{a,M} \cdot 1.60 = 14.4A \\ U - R_a I_{a,start} - E - R_p I_{a,start} &= 0 \Rightarrow R_p = \frac{220 - 0 - 2 \cdot 14.4}{14.4} = 13.3\Omega\end{aligned}$$

d)

$$\eta = \frac{P_2}{P_1} = \frac{M \frac{2\pi n}{60}}{U \cdot I} = \frac{12.4 \cdot \frac{2\pi \cdot n}{60}}{220 \cdot 9.55} = 86.5\%$$

e) Vid märkdrift:

$$220 - 2 \cdot 9.0 - k_1 \phi \cdot 1400 - 0 \cdot 9.0 = 0 \Rightarrow k_1 \phi = \frac{202}{1400}$$

$M = k_2 \phi I_a$ . Halva momentet ger  $I_a = \frac{9.0}{2} = 4.5A$ .

$$220 - 2 \cdot 4.5 - k_1 \phi n - 0 \cdot 4.5 \Rightarrow 1462rpm$$

**Uppgift 4.** a)

$$n_1 = \frac{120}{f} p$$

Poltal 4 ger  $n_1 = 1500$ . Därför har maskinen 4 poler.

b)

$$P_{2a} \approx P_2 = \frac{n_2 \cdot 2\pi}{60} M = \frac{1450 \cdot 2\pi \cdot 1235}{60} = 187.5 \text{ kW}$$

c)

$$P_1 = \frac{P_2}{\eta} = \frac{187500}{0.94} = 199.5 \text{ kW}$$
$$P_L = P_1 - P_2 = 199.5 - 187.5 = 12 \text{ kW}$$

d) Se föreläsningssanteckningar

e)

$$M = k_1 U^2 \frac{s}{R_2}$$
$$\frac{M_I}{M_{II}} = \frac{k_1 U^2 \frac{s_I}{R_2}}{k_1 U^2 \frac{s_{II}}{R_2}} \Rightarrow \frac{M_I}{M_{II}} = \frac{s_I}{s_{II}}$$
$$s_{II} = s_{II} \frac{M_{II}}{M_I} = \frac{n_s - n_I}{n_s} \frac{M_{II}}{M_I} = \frac{1500 - 1450}{1500} \frac{1235}{1235} = 0.024$$
$$n_{II} = n_s - s_{II} n_I = 1464 \text{ rpm}$$

f) Se boken eller föreläsningssanteckningar.

**Uppgift 5.** b)

$$U_L = \frac{6}{T} \int_{\frac{5T}{36}}^{\frac{17T}{36}} u(t) dt = \frac{6\omega}{2\pi} \int_{\frac{5\pi}{18\omega}}^{\frac{17\pi}{18\omega}} u(t) dt = \frac{3\omega}{\pi} \int_{\frac{5\pi}{18\omega}}^{\frac{17\pi}{18\omega}} \hat{u} \sin(\omega t) dt =$$
$$= \frac{3\omega}{\pi} \hat{u} \left[ -\frac{\cos(\omega t)}{\omega} \right]_{\frac{5\pi}{18\omega}}^{\frac{17\pi}{18\omega}} = \frac{3}{\pi} \hat{u} \left( -\cos\left(\frac{17\pi}{18}\right) + \cos\left(\frac{5\pi}{18}\right) \right)$$
$$= \frac{3}{\pi} \cdot \frac{400}{\sqrt{3}} \cdot \sqrt{2} \cdot (0.984 + 0.643) = 507.4 \text{ V}$$

c) Den likriktade spänningen är identisk oavsett om en induktiv eller en resistiv last används.