Vehicle Propulsion Systems Lecture 10

Case Study 6 Fuel Cell Vehicle and Optimal Control

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Outline

Repetition

Case study 6: Fuel Optimal Trajectories of a Racing FCEV Model compilation

Model simplification

Formulating the optimal control problem

Optimal Controllers Solutions

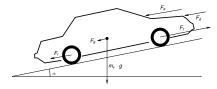
Some Additional Material – Fuel Consumption

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The Vehicle Motion Equation

Newtons second law for a vehicle

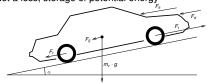
$$m_{V} \frac{d}{dt} v(t) = F_{t}(t) - (F_{a}(t) + F_{r}(t) + F_{g}(t) + F_{d}(t))$$



- ► F_t tractive force
- ► F_a aerodynamic drag force
- ▶ F_r rolling resistance force
- ▶ F_g gravitational force
- ► F_d disturbance force

Gravitational Force

Gravitational load force
 Not a loss, storage of potential energy



▶ Up- and down-hill driving produces forces.

$$F_g = m_v g \sin(\alpha)$$

Flat road assumed $\alpha=0$ if nothing else is stated (In the book).

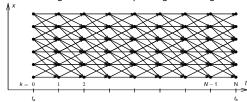
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Deterministic Dynamic Programming - Basic algorithm

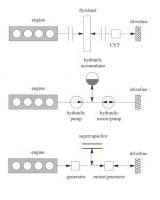
$$J(x_0) = g_N(x_N) + \sum_{k=0}^{N-1} g_k(x_k, u_k)$$
$$x_{k+1} = f_k(x_k, u_k)$$

Algorithm idea:

Start at the end and proceed backward in time to evaluate the optimal cost-to-go and the corresponding control signal



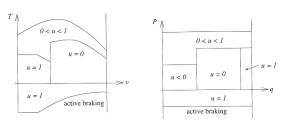
Examples of Short Term Storage Systems



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Heuristic Control Approaches

Parallel hybrid vehicle (electric assist)

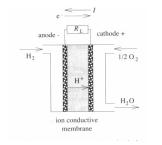


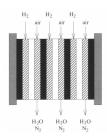
Determine control output as function of some selected state variables:

vehicle speed, engine speed, state of charge, power demand, motor speed, temperature, vehicle acceleration, torque demand

Fuel Cell Basic Principles

- ► Convert fuel directly to electrical energy
- Let an ion pass from an anode to a cathode
- ► Take out electrical work from the electrons
- ▶ Fuel cells are stacked ($U_{cell} \le 1V$)





Overview of Different Fuel Cell Technologies

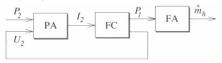
•				
Anode waste H ₂ , H ₂ O, CO ₂ ←				Cathode waste O ₂ , N ₂ , H ₂ O, CO ₂
112,1120,002				
AFC	H ₂ → H ₂ O ←	OH⁻ ≺	← Ο ₂	T=80 C
PEMFC PAFC	H ₂ →	H ⁺ →	← 0 ₂ → H ₂ O	T=80 C (PEMFC) T=200 C (PAFC)
MCFC	H ₂ → CO ₂ ←	CO ₃ ²⁻ ≺	← 0 ₂ → CO ₂	T=650 C
SOFC	H ₂ → H ₂ O ←	0 ² · ←	← O ₂	T=1000 C
Fuel H ₂ (+ CO ₂)	Apada	Slectrobito	√	Oxidant O ₂ (+ N ₂ , + CO ₂)

Hydrogen Fuel Storage

- Hydrogen storage is problematic Challenging task.
- Some examples of different options.
 - ▶ High pressure bottles
 - ► Liquid phase Cryogenic storage, -253°C.
 - Metal hydride
 - ► Sodium borohydride NaBH₄

Quasistatic Modeling of a Fuel Cell

Causality diagram



- ► Power amplifier (Current controller)
- ► Fuel amplifier (Fuel controller)
- ► Standard modeling approach

Fuel Cell Thermodynamics

Starting point reaction equation

$$H_2 + \frac{1}{2} O_2 \Rightarrow 2 H_2 0$$

Open system energy – Enthalpy H

$$H = U + pV$$

Reversible energy – Gibbs free energy G

$$G = H + TS$$

► Open circuit cell voltages

$$\textit{U}_{\textit{rev}} = -\frac{\Delta \textit{G}}{\textit{n}_{\textit{e}} \, \textit{F}}, \qquad \qquad \textit{U}_{\textit{id}} = -\frac{\Delta \textit{H}}{\textit{n}_{\textit{e}} \, \textit{F}},$$

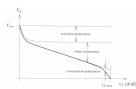
F – Faradays constant ($F = q N_0$)

Under load

$$P_{l} = I_{fc}(t) \left(U_{id} - U_{fc}(t) \right)$$

Fuel Cell Performance - Polarization curve

Polarization curve of a fuel cell Relating current density $i_{fc}(t) = I_{fc}(t)/A_{fc}$, and cell voltage $U_{fc}(t)$



Curve for one operating condition

- ▶ Fundamentally different compared to combustion engine/electrical motor
- Excellent part load behavior
- -When considering only the cell

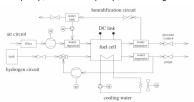
Fuel Cell System Modeling

▶ Describe all subsystems with models

$$P_2(t) = P_{st}(t) - P_{aux}(t)$$

$$P_{aux} = P_0 + P_{em}(t) + P_{ahp}(t) + P_{hp}(t) + P_{cl}(t) + P_{cf}(t)$$

em-electric motor, ahp - humidifier pump, hp - hydrogen recirculation pump, cl - coolant pump, cf - cooling fan.



▶ Submodels for: Hydrogen circuit, air circuit, water circuit, and coolant circuit

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Problem Setup

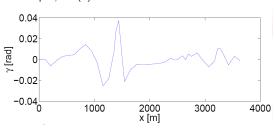
Run a fuel cell vehicle optimally on a racetrack



- Start up lapRepeated runs on the track
- Path to the solution
 - Measurements Model
 - Simplified model
 - Optimal control solutions

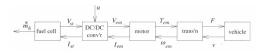
Problem Setup - Road Slope Given

Road slope $\gamma = \alpha(x)$



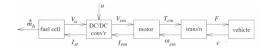
Model Causality

Model causality - Dynamic model



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Model Component - Fuel Cell



Current in the cell and losses

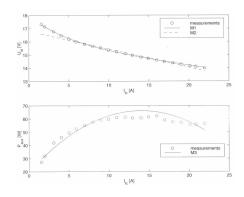
$$I_{fc}(t) = I_{fc}(t) + I_{aux}(t)$$

Current and hydrogen flow

$$\dot{m}_H(t) = c_9 I_{fc}(t)$$

▶ Next step: Polarization curve and auxiliary consumption

Fuel Cell - Polarization and Auxiliary Components



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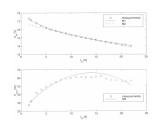
Fuel Cell - Polarization and Auxiliary Components

▶ Polarization curve

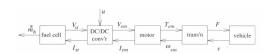
$$U_{st}(t) = c_0 + c_1 \cdot e^{-c_2 \cdot I_{fc}(t)} - c_3 \cdot I_{fc}(t)$$

Auxiliary power

$$P_{aux}(t) = c_6 + c_7 \cdot I_{fc}(t) + c_8 \cdot I_{fc}(t)$$



Model Component - DC Motor Controller



► DC motor voltage (from control signal *u*)

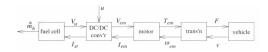
$$U_{em}(t) = \kappa \, \omega_{em}(t) + K \, R_{em} \, u(t)$$

Current requirement at the stack

$$I_{st} = \frac{U_{em}(t)I_{em}(t)}{\eta_c U_{st}(t)}$$

Model Component - Transmission and Wheels

Model Component - DC Motor



▶ DC motor current

$$I_{em}(t) = rac{U_{em}(t) - \kappa \, \omega_{em}(t)}{R_{em}}$$

▶ DC motor torque

$$T_{em}(t) = \kappa_{em} I_{em}(t)$$

Tractive force

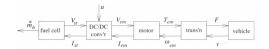
$$F(t) = \eta_t^{\pm 1} \, rac{\gamma \, T_{em}(t)}{r_w}$$

Rotational speed

$$\omega_{em}(t) = \frac{\gamma \ v(t)}{r_w}$$

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Model Compilation 1 - Vehicle



▶ The vehicle tractive force can now be expressed as

$$F(t) = rac{\eta_t \, \gamma}{r_{\!\scriptscriptstyle W}} \, \kappa_{em} \, K \, u(t)$$

▶ Dynamic vehicle velocity and position model

$$\frac{d}{dt}v(t) = h_1 u(t) - h_2 v^2(t) - g_0 - g_1 \alpha(x(t))$$
$$\frac{d}{dt}x(t) = v(t)$$

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Model Compilation 2 – Fuel Consumption



Fuel flow, $\dot{m}_H(t) = c_9 I_{fc}(t)$

$$I_{fc}(t) = \frac{P_{aux}(I_{st}(t))}{U_{st}(I_{st}(t))} + \frac{K \ u(t)}{\eta_c \ U_{st}(I_{st}(t))} \left(K \ R_{em} \ u(t) + \kappa_{em} \frac{\gamma}{r_w} \ v(t) \right)$$

-Implicit nonlinear static function

▶ Simpler model

$$\dot{m}_H(t) = b_0 + b_1 v(t) u(t) + b_2 u^2(t)$$

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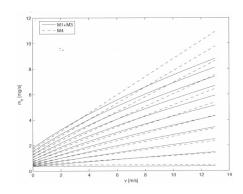
Model simplification

Formulating the optimal control problem

Optimal Controllers Solutions

Some Additional Material – Fuel Consumption

Simplified Fuel Consumption - Validation



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Detour

- Occam's razor:
 - $-\mbox{The}$ explanation of any phenomenon should make as few assumptions as possible.

Shave of those who are unnecessary.

- Law of Parsimony: Among others a factor in statistics: In general, mathematical models with the smallest number of parameters are preferred as each parameter introduced into the model adds some uncertainty to it.
- Another viewpoint.

Try to simplify the problem you solve as much as possible.

-Neglect effects and be proud when you are successful!

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Optimal Control Problems

► Start of the cycle

$$v(0) = 0, \quad x(0) = 0$$

$$\lambda_1(t_f) = 0, \qquad x(t_f) = x_f = v_m t_f$$

► Periodic route

$$x(0) = 0$$

$$\lambda_1(t_f) = \lambda_1(0), \qquad x(t_f) = x_f = v_m t_f, \qquad v(t_f) = v(0)$$

PID Cruise Controller - Baseline for Comparison

Simple controller for the start

$$u(t) = K_p(f v_m - v(t)) + K_i \int_0^t (f v_m - v_t(t)) dt$$

f-tuning parameter ≈ 1 to allow for matching the average speed

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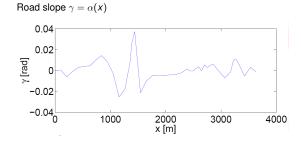
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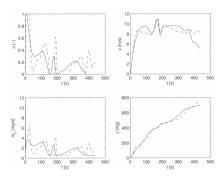
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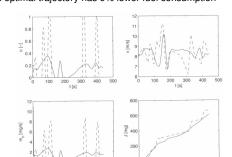
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Fuel Optimal Trajectory - Start

Fuel optimal trajectory has 7% lower fuel consumption



Fuel Optimal Trajectory – Continuous Driving
Fuel optimal trajectory has 9% lower fuel consumption



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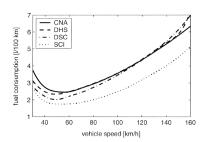
Formulating the optimal control problem

Optimal Controllers Solutions

Some Additional Material – Fuel Consumption

Fuel Optimal Speed for Normal Driving

ICE vehicle (light weight 800 kg)



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Engine Map an Gearbox Layout

CI engine (light weight 800 kg)

