Vehicle Propulsion Systems Lecture 6

Supervisory Control Algorithms

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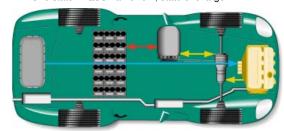
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Outline

Repetition

Hybrid Electrical Vehicles - Parallel

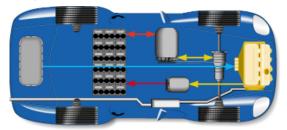
- ► Two parallel energy paths
- One state in QSS framework, state of charge



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Hybrid Electrical Vehicles - Serial

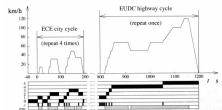
- ► Two paths working in parallel
- Decoupled through the battery
- ► Two states in QSS framework, state of charge & Engine speed



Optimization, Optimal Control, Dynamic Programming

What gear ratios give the lowest fuel consumption for a given drivingcycle?

-Problem presented in appendix 8.1



Problem characteristics

- Countable number of free variables, $i_{g,j}, j \in [1, 5]$
- ▶ A "computable" cost, $m_f(\cdots)$
- A "computable" set of constraints, model and cycle
- ► The formulated problem

 $m_f(i_{g,1},i_{g,2},i_{g,3},i_{g,4},i_{g,5})$

model and cycle is fulfilled s.t.

General problem formulation

▶ Performance index

$$J(u) = \phi(x(t_b), t_b) + \int_{t_a}^{t_b} L(x(t), u(t), t) dt$$

System model (constraints)

$$\frac{d}{dt}x = f(x(t), u(t), t), x(t_a) = x_a$$

State and control constraints

$$u(t) \in U(t)$$

$$x(t) \in X(t)$$

Optimal Control - Problem Motivation

Car with gas pedal u(t) as control input: How to drive from A to B on a given time with minimum fuel consumption?

- ▶ Infinite dimensional decision variable u(t).
- ► Cost function $\int_0^{t_f} \dot{m}_f(t) dt$
- ▶ Constraints:
 - Model of the car (the vehicle motion equation)

$$m_V \frac{d}{dt} v(t) = F_t(v(t), u(t)) - (F_a(v(t)) + F_r(v(t)) + F_g(x(t)))$$

$$\frac{d}{dt} x(t) = v(t)$$

$$\dot{m}_t = f(v(t), u(t))$$

- ▶ Starting point x(0) = A
- End point $x(t_f) = B$
- Speed limits $v(t) \le g(x(t))$
- ▶ Limited control action $0 \le u(t) \le 1$

Dynamic programming - Problem Formulation

► Optimal control problem

$$\begin{aligned} & \min J(u) = \phi(x(t_b), t_b) + \int_{t_a}^{t_b} L(x(t), u(t), t) dt \\ & s.t. \ \frac{d}{dt} x = f(x(t), u(t), t) \\ & \quad x(t_a) = x_a \\ & \quad u(t) \in U(t) \\ & \quad x(t) \in X(t) \end{aligned}$$

- ▶ x(t), u(t) functions on $t \in [t_a, t_b]$
- Search an approximation to the solution by discretizing
 - ▶ the state space *x*(*t*)
 - and maybe the control signal u(t)

in both amplitude and time.

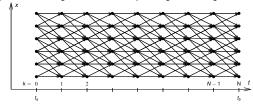
► The result is a combinatorial (network) problem

Deterministic Dynamic Programming - Basic algorithm

$$J(x_0) = g_N(x_N) + \sum_{k=0}^{N-1} g_k(x_k, u_k)$$
$$x_{k+1} = f_k(x_k, u_k)$$

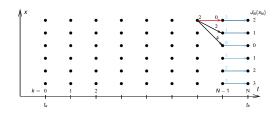
Algorithm idea:

Start at the end and proceed backwards in time to evaluate the optimal cost-to-go and the corresponding control signal.



Deterministic Dynamic Programming – Basic Algorithm

Graphical illustration of the solution procedure



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Arc Cost Calculations

There are two ways for calculating the arc costs

- Calculate the exact control signal and cost for each arc.
 Quasi-static approach
- Make a grid over the control signal and interpolate the cost for each arc.

-Forward calculation approach

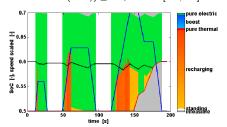
Matlab implementation – it is important to utilize matrix calculations

- ▶ Calculate the whole bundle of arcs in one step
- Add boundary and constraint checks

2D and 3D grid examples on whiteboard

Parallel Hybrid Example

- ► Fuel-optimal torque split factor $u(SOC, t) = \frac{T_{e-motor}}{T_{gearbox}}$
- ► ECE cycle
- ▶ Constraints $SOC(t = t_f) \ge 0.6$, $SOC \in [0.5, 0.7]$



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Outline

Repetition

Supervisory Control Algorithms

Heuristic Control Approaches

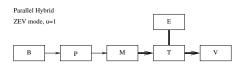
Optimal Control Strategies

Analytical solutions to Optimal Control Problems ECMS – Equivalent Consumption Minimization Strategy Parallel Hybrid - Modes and Power Flows

The different modes for a parallel hybrid

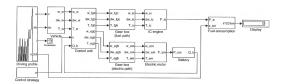
 $u \approx P_{batt}/P_{vehicle}$

Battery drive mode (ZEV)



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Control algorithms



Determining the power split ratio u

$$u_{j}(t) = \frac{P_{j}(t)}{P_{m+1}(t) + P_{l}(t)}$$
(4.110)

- ▶ Clutch engagement disengagement $B_c \in \{0, 1\}$
- \blacktriangleright Engine engagement disengagement $\textit{B}_{\textit{e}} \in \{0,1\}$

Strategies for the Parallel Hybrid

Power split u, Clutch B_c , Engine B_e

| | Mode | и | B_e | B_c |
|----|----------------------|-------|-------|-------|
| 1 | ICE | 0 | 1 | 1 |
| 2a | ZEV | 1 | 0 | 0 |
| 2b | ZEV | 1 | 0 | 1 |
| 3 | Power assist | [0,1] | 1 | 1 |
| 4 | Recharge | < 0 | 1 | 1 |
| 5a | Regenerative braking | 1 | 0 | 0 |
| 5a | Regenerative braking | 1 | 0 | 1 |

All practical control strategies have engine shut off when the torque at the wheels are negative or zero; standstill, coasting and braking.

Classification I - Supervisory Control Algorithms

- Non-causal controllers
 - Detailed knowledge about future driving conditions.
 - Position, speed, altitude, traffic situation.

Regulatory drive cycles, public transportation, long haul operation, GPS based route planning.

- Causal controllers
 - No knowledge about the future..
 - Use information about the current state.
 - Uses:

"The normal controller", on-line, in vehicles without planning

- ► Heuristic controllers
 - -Causal
 - -State of the art in most prototypes and mass-production
- Optimal controllers
 - -Often non-causal
- -Solutions exist for simplifications

Classification II - Vehicle Controllers

- Sub-optimal controllers
 - -Often causal

On-going work to include optimal controllers in prototypes

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Some Comments About the Problem

- Difficult problem
- Unsolved problem for causal controllers
- Rich body of engineering reports and research papers on the subject

-This can clearly be seen when reading chapter 7!

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Heuristic Control Approaches

Heuristic Control Approaches

Operation usually depends on a few vehicle operation

Rule based:

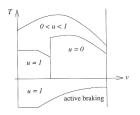
Nested if-then-else clauses if $v < v_{low}$ then use electric motor (u=1). else...

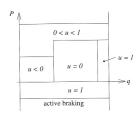
Fuzzy logic based

Classification of the operating condition into fuzzy sets. Rules for control output in each mode. Defuzzyfication gives the control output.

Heuristic Control Approaches

► Parallel hybrid vehicle (electric assist)





 Determine control output as function of some selected state variables:

vehicle speed, engine speed, state of charge, power demand, motor speed, temperature, vehicle acceleration, torque demand.

Heuristic Control Approaches - Concluding Remarks

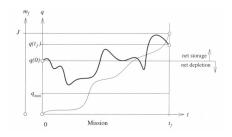
- ► Easy to conceive
- ► Relatively easy to implement
- ► Result depends on the thresholds
- ▶ Proper tuning can give good fuel consumption reduction and charge sustainability
- ▶ Performance varies with cycle and driving condition -Not robust
- Time consuming to develop an tune for advanced hybrid configurations

Outline

Optimal Control Strategies

Consider a driving mission

Variables. Control signal – u(t), System state – x(t), State of charge q(t) (is a state).



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Formulating the Optimal Control Problem

-What is the optimal behaviour? Defines Performance index J.

▶ Minimize the fuel consumption

$$J = \int_0^{t_f} \dot{m}_f(t, u(t)) dt$$

▶ Balance between fuel consumption and emissions

$$J = \int_0^{t_f} \left[\dot{m}_f(t, u(t)) + \alpha_{CO} \dot{m}_{CO}(x(t), u(t)) + \alpha_{NO} \dot{m}_{NO}(x(t), u(t)) + \alpha_{HC} \dot{m}_{HC}(x(t), u(t)) \right] dt$$

► Include driveability criterion

$$J = \int_0^{t_f} \dot{m}_f(t, u(t)) + \beta \left(\frac{d}{dt} a(t)\right)^2 dt$$

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First Solution to the Problem

▶ Minimize the fuel consumption

$$J = \int_0^{t_f} \dot{m}_f(t, u(t)) dt$$

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Including constraints

► Hard or soft constraints

$$min J(u) = \int_0^{t_f} L(t, u(t)) dt$$
s.t. $q(0) = q(t_f)$

$$\min \ J(u) = \phi(q(t_f)) + \int_0^{t_f} L(t, u(t)) dt$$

▶ How to select $\phi(q(t_f))$?

$$\phi(q(t_f)) = \alpha (q(t_f) - q(0))^2$$

penalizes high deviations more than small, independent of sign

$$\phi(q(t_f)) = w(q(0) - q(t_f))$$

penalizes battery usage, favoring energy storage for future use

One more feature from the last one

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Including constraints

► Including battery penalty according to

$$\phi(q(t_f)) = w(q(0) - q(t_f)) = -w \int_0^{t_f} \dot{q}(t)dt$$

enables us to rewrite

$$\min \ J(u) = \int_0^{t_f} L(t, u(t)) - w \, \dot{q}(t) dt$$

Constraints That are Also Included

► State equation $\dot{x} = f(x)$ is also included – From Lecture 5

Consider hybrid with only one state, SoC

$$\begin{aligned} \min J(u) &= \phi(q(t_f), t_f) + \int_0^{t_f} L(t, u(t)) dt \\ s.t. & \frac{d}{dt}q = f(t, q(t), u(t)) \\ & u(t) \in U(t) \\ & q(t) \in Q(t) \end{aligned}$$

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Outline

Repetition

Supervisory Control Algorithms

Heuristic Control Approaches

Optimal Control Strategies

Analytical solutions to Optimal Control Problems

ECMS – Equivalent Consumption Minimization Strategy

Analytical Solutions to Optimal Control Problems

► Core of the problem

$$\min J(u) = \phi(q(t_f), t_f) + \int_0^{t_f} L(t, u(t)) dt$$

$$s.t. \ \dot{q}(t) = f(t, q(t), u(t))$$

► Hamiltonian from optimal control theory

$$H(t, q(t), u(t), \mu(t)) = L(t, u(t)) + \mu(t) f(t, q(t), u(t))$$

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Analytical Solutions to Optimal Control Problems

► Hamiltonian

$$H(t, q(t), u(t), \mu(t)) = L(t, u(t)) + \mu(t) f(t, q(t), u(t))$$

► Solution (theory from Appendix B)

$$u(t) = \underset{u}{\operatorname{arg\,min}} H(t, q(t), u(t), \mu(t))$$

with

$$\dot{\mu}(t) = -\frac{\partial}{\partial q} f(t, q(t), u(t))$$
$$\dot{q}(t) = f(t, q(t), u(t))$$

• If $\frac{\partial}{\partial q}f(t,q(t),u(t))=0$ the problem becomes simpler μ becomes a constant μ_0 , search for it when solving

Analytical Solutions to Optimal Control Problems

 \blacktriangleright μ_0 depends on the (soft) constraint

$$\mu_0 = rac{\partial}{q(t_{\!f})}\phi(q(t_{\!f})) = /{\sf special\ case}/ = -{\it w}$$

▶ Different efficiencies

$$\mu_0 = \frac{\partial}{\partial q(t_f)} \phi(q(t_f)) = \begin{cases} -\textit{w}_{\textit{dis}}, & q(t_f) > q(0) \\ -\textit{w}_{\textit{chg}}, & q(t_f) < q(0) \end{cases}$$

 Introduce equivalence factor (scaling) by studying battery and fuel power

$$s(t) = -\mu(t) rac{H_{LHV}}{V_b \, Q_{max}}$$

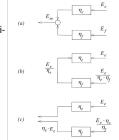
ECMS - Equivalent Consumption Minimization Strategy

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Determining Equivalence Factors I

Constant engine and battery efficiencies

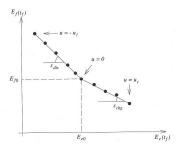
$$egin{aligned} oldsymbol{s}_{ extit{dis}} &= rac{1}{\eta_e\,\eta_f} \ oldsymbol{s}_{ extit{chg}} &= rac{\eta_e}{\eta_f} \end{aligned}$$



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Determining Equivalence Factors II

► Collecting battery and fuel energy data from test runs with constant *u* gives a graph

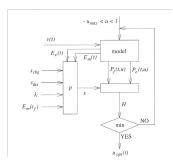


► Slopes determine s_{dis} and s_{chg}.

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ECMS On-line Implementation

Flowchart



There is also a T-ECMS (telemetry-ECMS)

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