Vehicle Propulsion Systems Lecture 6

Non Electric Hybrid Propulsion Systems

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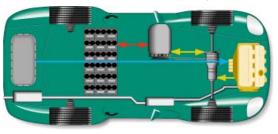
Vehicular Systems Linköping University

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Hybrid Electrical Vehicles - Parallel

- Two parallel energy paths
- One state in QSS framework, state of charge

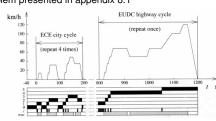


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Optimization, Optimal Control, Dynamic Programming What gear ratios give the lowest fuel consumption for a given

drivingcycle? -Problem presented in appendix 8.1



Problem characteristics

- Countable number of free variables, $i_{g,j}, j \in [1, 5]$
- A "computable" cost, $m_f(\cdots)$
- A "computable" set of constraints, model and cycle
- The formulated problem

 $m_f(i_{g,1}, i_{g,2}, i_{g,3}, i_{g,4}, i_{g,5})$

 $\min_{i_{g,j}, j \in [1,5]}$ model and cycle is fulfilled s.t.

General problem formulation

Performance index

$$J(u) = \phi(x(t_b), t_b) + \int_{t_a}^{t_b} L(x(t), u(t), t) dt$$

System model (constraints)

$$\frac{d}{dt}x = f(x(t), u(t), t), x(t_a) = x_a$$

State and control constraints

$$u(t) \in U(t)$$

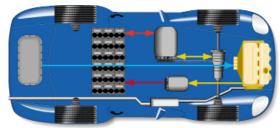
 $x(t) \in X(t)$

Outline

Repetition

Hybrid Electrical Vehicles - Serial

- Two paths working in parallel
- Decoupled through the battery
- Two states in QSS framework, state of charge & Engine speed



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Optimal Control – Problem Motivation

Car with gas pedal u(t) as control input:

How to drive from A to B on a given time with minimum fuel consumption?

- Infinite dimensional decision variable u(t).
- Cost function $\int_0^{t_f} \dot{m}_f(t) dt$
- Constraints:

Model of the car (the vehicle motion equation)

$$\begin{array}{lll} m_{v}\frac{d}{dt}v(t) &= F_{t}(v(t), u(t)) & -(F_{a}(v(t)) + F_{r}(v(t)) + F_{g}(x(t))) \\ \frac{d}{dt}x(t) &= v(t) \\ \dot{m}_{t} &= f(v(t), u(t)) \end{array}$$

- Starting point x(0) = A
- End point $x(t_f) = B$
- Speed limits $v(t) \leq g(x(t))$
- Limited control action $0 \le u(t) \le 1$

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Dynamic programming – Problem Formulation

Optimal control problem

min
$$J(u) = \phi(x(t_b), t_b) + \int_{t_a}^{t_b} L(x(t), u(t), t) dt$$

s.t. $\frac{d}{dt}x = f(x(t), u(t), t)$
 $x(t_a) = x_a$
 $u(t) \in U(t)$
 $x(t) \in X(t)$

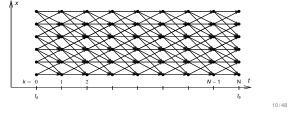
- ▶ x(t), u(t) functions on $t \in [t_a, t_b]$
- Search an approximation to the solution by discretizing ► the state space x(t)
 - and maybe the control signal u(t)in both amplitude and time.
- The result is a combinatorial (network) problem

Deterministic Dynamic Programming - Basic algorithm

$$J(x_0) = g_N(x_N) + \sum_{k=0}^{N-1} g_k(x_k, u_k)$$
$$x_{k+1} = f_k(x_k, u_k)$$

Algorithm idea:

Start at the end and proceed backwards in time to evaluate the optimal cost-to-go and the corresponding control signal.



Arc Cost Calculations

There are two ways for calculating the arc costs

- Calculate the exact control signal and cost for each arc. –Quasi-static approach
- Make a grid over the control signal and interpolate the cost for each arc.
- -Forward calculation approach

- Calculate the whole bundle of arcs in one step
- Add boundary and constraint checks

2D and 3D grid examples on whiteboard

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Outline

Repetition

Short Term Storage

lybrid-Inertial Propulsion Systems Basic principles Design principles Modeling Continuously Variable Transmission

Hybrid-Hydraulic Propulsion Systems

Modeling

Hydraulic Pumps and Motors

Pneumatic Hybrid Engine Systems

Case studies

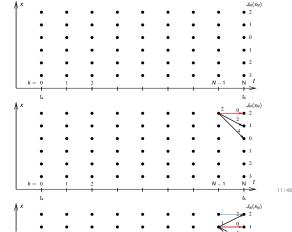
Short Term Storage - F1

FIA allowed the usage of 60 kW, KERS (Kinetic Energy Recovery System) in F1 in 2009. Technologies:

- Flywheel
- Batteries
- Balleries
- Super-Caps

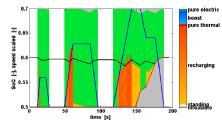
Deterministic Dynamic Programming – Basic Algorithm

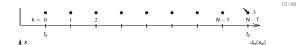
Graphical illustration of the solution procedure



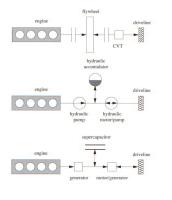
Parallel Hybrid Example

- Fuel-optimal torque split factor $u(SOC, t) = \frac{T_{e-motor}}{T_{acorbar}}$
- ECE cycle
- ▶ Constraints $SOC(t = t_f) \ge 0.6$, $SOC \in [0.5, 0.7]$





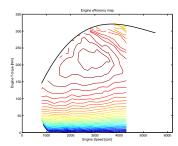
Examples of Short Term Storage Systems





Basic Principles for Hybrid Systems

- Kinetic energy recovery
 - Use "best" points Duty cycle.
 - Run engine (fuel converter) at its optimal point.Shut-off the engine.

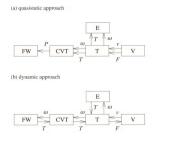


Power and Energy Densities

Asymptotic power and energy density – The Principle

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Causality for a hybrid-inertial propulsion system



Flywheel accumulator – Design principle

Energy stored (SOC):

$$E_f = rac{1}{2} \Theta_f \omega_f^2$$

Wheel inertia

$$\Theta_f = \rho \, b \, \int_{Area} r^2 \, 2 \, \pi \, r \, dr = \ldots = \frac{\pi}{2} \, \rho \, \frac{d^4}{16} \, (1 - q^4)$$

- Wheel Mass
- $m_f = \pi \,
 ho \, b \, d^2 \, (1 q^2)$
- Energy to mass ratio

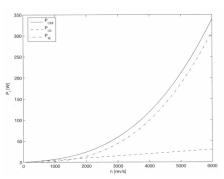
$$\frac{E_f}{m_f} = \frac{d^2}{16}(1+q^2)\omega_f^2 = \frac{u^2}{4}(1+q^2)$$

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Power losses as a function of speed

Air resistance and bearing losses



Outline

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Hybrid-Hydraulic Propulsion Systems Basics

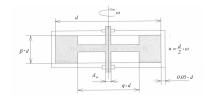
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Flywheel accumulator



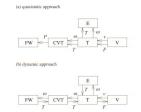
• Energy stored ($\Theta_f = J_f$):



Wheel inertia

$$\Theta_t = \rho \, b \, \int_{Area} r^2 \, 2 \, \pi \, r \, dr = \ldots = \frac{\pi}{2} \, \rho \, \frac{d^4}{16} \, (1 - q^4)$$

Quasistatic Modeling of FW Accumulators

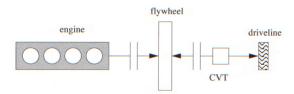


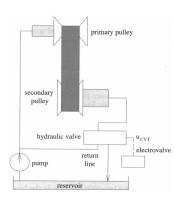
Flywheel speed (SOC) $P_2(t)$ – power out, $P_l(t)$ – power loss

$$\Theta_f \omega_2(t) \frac{d}{dt} \omega_2(t) = -P_2(t) - P_l(t)$$

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Continuously Variable Transmission (CVT)





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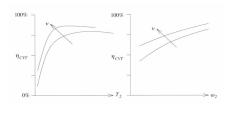
CVT Modeling

 Transmission (gear) ratio v, speeds and transmitted torques

$$\omega_1(t) = \nu(t) \,\omega_2(t)$$

$$T_{t1}(t) = \nu \left(T_{t2}(t) - T_l(t)\right)$$

 An alternative to model the losses, is to use an efficiency definition.



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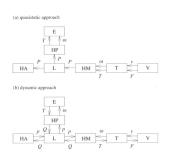
Hydraulic Pumps and Motors

Pneumatic Hybrid Engine Systems

Case studies

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Causality for a hybrid-hydraulic propulsion system



CVT Modeling

 Transmission (gear) ratio v, speeds and transmitted torques

$$\omega_1(t) = \nu(t) \,\omega_2(t)$$

$$T_{t1}(t) = \nu \left(T_{t2}(t) - T_l(t)\right)$$

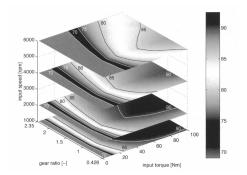
Newtons second law for the two pulleys

$$\Theta_1 \frac{\partial}{\partial t} \omega_1(t) = T_1(t) - T_{t1}(t)$$
$$\Theta_2 \frac{\partial}{\partial t} \omega_2(t) = T_2(t) - T_{t2}(t)$$

System of equations give

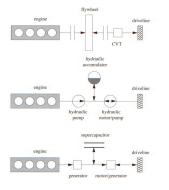
$$T_{1}(t) = T_{l}(t) + \frac{T_{2}(t)}{\nu(t)} + \frac{\Theta_{CVT}(t)}{\nu(t)} \frac{d}{dt} \omega_{2}(t) + \Theta_{1} \frac{d}{dt} \nu(t) \omega_{2}(t)$$
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Efficiencies for a Push-Belt CVT



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Examples of Short Term Storage Systems



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Modeling of a Hydraulic Accumulator

Modeling principle –Energy balance

$$m_g c_v \frac{d}{dt} \theta_g(t) = -\rho \frac{d}{dt} V_g(t) - h A_w \left(\theta_g(t) - \theta - M_{w} \right)$$
-Mass balance

$$\frac{d}{dt}V_g(t)=Q_2(t)$$

-Ideal gas law

$$p_g(t) = rac{m_g \, R_g \, heta_g(t)}{V_g(t)}$$



Power generation

 $P_2(t)=p_2(t)\,Q_2(t)$

Model Simplification

Simplifications made in thermodynamic equations to get a simple state equation.

Assuming steady state conditions.
 –Eliminating θ_g and the volume change gives

$$p_2(t) = \frac{h A_w \theta_w m_g R_g}{V_g(t) h A_w + m_g R_g Q_2(t)}$$

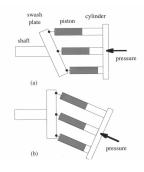
Combining this with the power output gives

$$Q_{2}(t) = \frac{V_{g}(t)}{m_{g}} \frac{h A_{w} P_{2}(t)}{R_{g} \theta_{w} h A_{w} - R_{g} P_{2}(t)}$$

- Integrating $Q_2(t)$ gives V_g as the state in the model.
- Modeling of the hydraulic systems efficiency, see the book.
 A detail for the assignment
- -This simplification can give problems in the simulation if parameter values are off. (Division by zero.)

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Hydraulic Pumps



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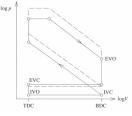
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Conventional SI Engine

Compression and expansion model

$$p(t) = c v(t)^{-\gamma} \qquad \Rightarrow \qquad \log(p(t)) = \log(c) - \gamma \log(v(t))$$

gives lines in the log-log diagram version of the pV-diagram



Outline

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- Hybrid-Inertial Propulsion System
 - Basic prin
 - Design pr
 - Continuously Variable Transmission

Hybrid-Hydraulic Propulsion Systems

Modelin

Hydraulic Pumps and Motors

Pneumatic Hybrid Engine Systems

Modeling of Hydraulic Motors

Efficiency modeling

$$\begin{aligned} P_{1}(t) = & \frac{P_{2}(t)}{\eta_{hm}(\omega_{2}(t), T_{2}(t))}, \qquad P_{2}(t) > 0\\ P_{1}(t) = & P_{2}(t) \eta_{hm}(\omega_{2}(t), -|T_{2}|(t)), \qquad P_{2}(t) < 0 \end{aligned}$$

Willans line modeling, describing the loss

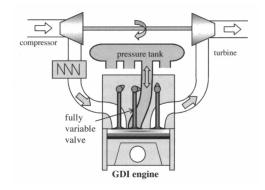
$$P_1(t)=\frac{P_2(t)+P_0}{e}$$

 Physical modeling Wilson's approach provided in the book.

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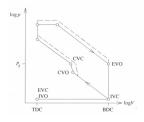
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Pneumatic Hybrid Engine System



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Super Charged Mode



Under Charged Mode

Outline

Case studies

Problem description

starting and stopping the engine -Minimize fuel consumption

log p

 P_t

EVC

TDC

Pneumatic Brake System



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Case Study 3: ICE and Flywheel Powertrain

- Control of a ICE and Flywheel Powertrain

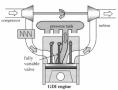
IV

log

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Case Study 8: Hybrid Pneumatic Engine

- Local optimization of the engine thermodynamic cycle
- Different modes to select between
- Dynamic programming of the mode selection



 $\overline{\omega}$ flywheel speed ω_f engine speed ω_e

For each constant vehicle speed find the optimal limits for

–Solved through parameter optimization \Rightarrow Map used for control

 $\tau_o \tau_c \quad \tau_c + \vartheta$

t

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