Vehicle Propulsion Systems Lecture 7

Non Electric Hybrid Propulsion Systems

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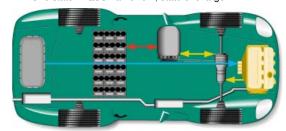
December 1, 2014

Outline

Repetition

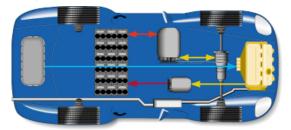
Hybrid Electrical Vehicles - Parallel

- ► Two parallel energy paths
- One state in QSS framework, state of charge



Hybrid Electrical Vehicles - Serial

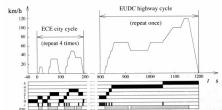
- ► Two paths working in parallel
- Decoupled through the battery
- ► Two states in QSS framework, state of charge & Engine speed



Optimization, Optimal Control, Dynamic Programming

What gear ratios give the lowest fuel consumption for a given drivingcycle?

-Problem presented in appendix 8.1



Problem characteristics

- Countable number of free variables, $i_{g,j}, j \in [1, 5]$
- ▶ A "computable" cost, $m_f(\cdots)$
- A "computable" set of constraints, model and cycle
- ► The formulated problem

 $m_f(i_{g,1},i_{g,2},i_{g,3},i_{g,4},i_{g,5})$ s.t.

model and cycle is fulfilled

General problem formulation

▶ Performance index

$$J(u) = \phi(x(t_b), t_b) + \int_{t_a}^{t_b} L(x(t), u(t), t) dt$$

System model (constraints)

$$\frac{d}{dt}x = f(x(t), u(t), t), x(t_a) = x_a$$

State and control constraints

$$u(t) \in U(t)$$

$$x(t) \in X(t)$$

Optimal Control - Problem Motivation

Car with gas pedal u(t) as control input: How to drive from A to B on a given time with minimum fuel consumption?

- ▶ Infinite dimensional decision variable u(t).
- ► Cost function $\int_0^{t_f} \dot{m}_f(t) dt$
- ▶ Constraints:
 - Model of the car (the vehicle motion equation)

model of the car (the venicle motion equation)
$$m_{\nu} \frac{d}{dt} v(t) = F_t(v(t), u(t)) - (F_a(v(t)) + F_r(v(t)) + F_g(x(t)))$$

$$\frac{d}{dt} x(t) = v(t)$$

$$\dot{m}_t = f(v(t), u(t))$$

- ▶ Starting point x(0) = A
- End point $x(t_f) = B$
- Speed limits $v(t) \le g(x(t))$
- ▶ Limited control action $0 \le u(t) \le 1$

Dynamic programming - Problem Formulation

► Optimal control problem

$$\begin{aligned} \min J(u) &= \phi(x(t_b), t_b) + \int_{t_a}^{t_b} L(x(t), u(t), t) dt \\ s.t. &\frac{d}{dt} x = f(x(t), u(t), t) \\ &x(t_a) = x_a \\ &u(t) \in U(t) \\ &x(t) \in X(t) \end{aligned}$$

- ▶ x(t), u(t) functions on $t \in [t_a, t_b]$
- Search an approximation to the solution by discretizing
 - ▶ the state space *x*(*t*)
 - and maybe the control signal u(t)

in both amplitude and time.

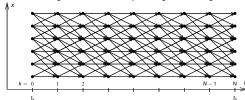
► The result is a combinatorial (network) problem

Deterministic Dynamic Programming - Basic algorithm

$$J(x_0) = g_N(x_N) + \sum_{k=0}^{N-1} g_k(x_k, u_k)$$
$$x_{k+1} = f_k(x_k, u_k)$$

Algorithm idea:

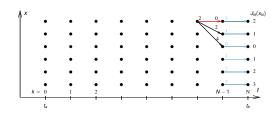
Start at the end and proceed backwards in time to evaluate the optimal cost-to-go and the corresponding control signal.



10/48

Deterministic Dynamic Programming – Basic Algorithm

Graphical illustration of the solution procedure



11/-

Arc Cost Calculations

There are two ways for calculating the arc costs

- Calculate the exact control signal and cost for each arc.
 Quasi-static approach
- Make a grid over the control signal and interpolate the cost for each arc.
 - -Forward calculation approach

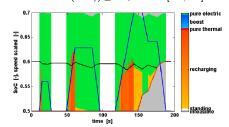
Matlab implementation – it is important to utilize matrix calculations

- ▶ Calculate the whole bundle of arcs in one step
- Add boundary and constraint checks

2D and 3D grid examples on whiteboard

Parallel Hybrid Example

- ► Fuel-optimal torque split factor $u(SOC, t) = \frac{T_{e-motor}}{T_{gearbox}}$
- ► ECE cycle
- ▶ Constraints $SOC(t = t_f) \ge 0.6$, $SOC \in [0.5, 0.7]$



13

Outline

Repetition

Short Term Storage

Hybrid-Inertial Propulsion Systems

Basic principles

Design principle

Modeling

Continuously Variable Transmission

Hybrid-Hydraulic Propulsion Systems

Basics

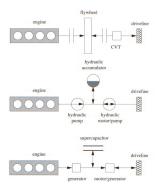
Modeling

Hydraulic Pumps and Motors

Pneumatic Hybrid Engine Systems

Case studies

Examples of Short Term Storage Systems



15/4

Short Term Storage - F1

2009 FIA allowed the usage of 60 kW, KERS (Kinetic Energy Recovery System) in F1.

Technologies:

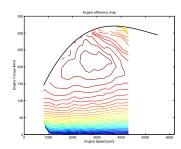
- ► Flywheel
- ► Super-Caps, Ultra-Caps
- Batteries

2014, will allow KERS units with 120 kilowatts (160 bhp).

–To balance the sport's move from 2.4 I V8 engines to 1.6 I V6 engines.

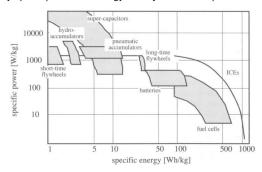
Basic Principles for Hybrid Systems

- Kinetic energy recovery
- ▶ Use "best" points Duty cycle.
 - ► Run engine (fuel converter) at its optimal point.
 - Shut-off the engine.



Power and Energy Densities

Asymptotic power and energy density - The Principle



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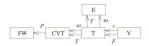
Pneumatic Hybrid Engine Systems

Case studies

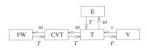
18/48

Causality for a hybrid-inertial propulsion system

(a) quasistatic approach

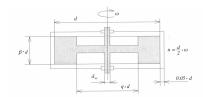


(b) dynamic approach



20/48

Flywheel accumulator



▶ Energy stored ($\Theta_f = J_f$):

$$E_f = \frac{1}{2} \Theta_f \, \omega_f^2$$

Wheel inertia

$$\Theta_f = \rho \, b \, \int_{Area} r^2 \, 2 \, \pi \, r \, dr = \ldots = \frac{\pi}{2} \, \rho \, b \, \frac{d^4}{16} \, (1 - q^4)$$

21/4

Flywheel accumulator - Design principle

► Energy stored (SOC):

$$E_f = \frac{1}{2} \Theta_f \omega_f^2$$

▶ Wheel inertia

$$\Theta_f = \rho \, b \, \int_{Area} r^2 \, 2 \, \pi \, r \, dr = \ldots = \frac{\pi}{2} \, \rho \, b \, \frac{d^4}{16} \, (1 - q^4)$$

Wheel Mass

$$m_f = \pi \, \rho \, b \, d^2 \, (1 - q^2)$$

► Energy to mass ratio

$$\frac{E_f}{m_f} = \frac{d^2}{16}(1+q^2)\omega_f^2 = \frac{u^2}{4}(1+q^2)$$

Quasistatic Modeling of FW Accumulators

(a) quasistatic approach



(b) dynamic approach

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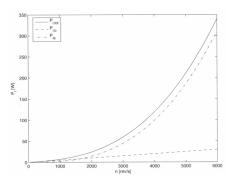
Flywheel speed (SOC) $P_2(t)$ – power out, $P_l(t)$ – power loss

$$\Theta_f \omega_2(t) \frac{d}{dt} \omega_2(t) = -P_2(t) - P_I(t)$$

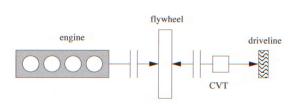
23/4

Power losses as a function of speed

Air resistance and bearing losses

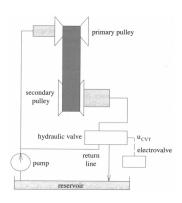


Continuously Variable Transmission (CVT)



24/48

CVT Principle



26/48

CVT Modeling

 \blacktriangleright Transmission (gear) ratio $\nu,$ speeds and transmitted torques

$$\omega_1(t) = \nu(t) \omega_2(t)$$

$$T_{t1}(t) = \nu \left(T_{t2}(t) - T_{t}(t) \right)$$

Newtons second law for the two pulleys

$$\Theta_1 \frac{d}{dt} \omega_1(t) = T_1(t) - T_{t1}(t)$$

$$\Theta_2 \frac{d}{dt} \omega_2(t) = T_2(t) - T_{t2}(t)$$

► System of equations give

$$\mathit{T}_{1}(t) = \mathit{T}_{l}(t) + \frac{\mathit{T}_{2}(t)}{\nu(t)} + \frac{\Theta_{CVT}(t)}{\nu(t)} \frac{d}{dt} \omega_{2}(t) + \Theta_{1} \frac{d}{dt} \nu(t) \, \omega_{2}(t)$$

27/40

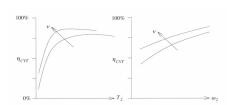
CVT Modeling

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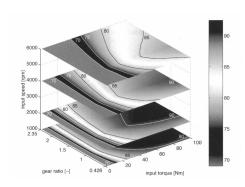
$$T_{t1}(t) = \nu \left(T_{t2}(t) - T_{t}(t) \right)$$

An alternative to model the losses, is to use an efficiency definition.



28/48

Efficiencies for a Push-Belt CVT



29/4

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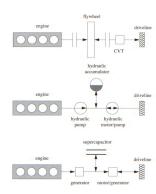
Modeling

Hydraulic Pumps and Motors

Pneumatic Hybrid Engine Systems

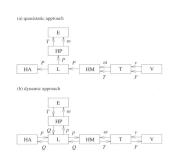
Case studies

Examples of Short Term Storage Systems



31/4

Causality for a hybrid-hydraulic propulsion system



Modeling of a Hydraulic Accumulator

Modeling principle
–Energy balance

 $m_g c_V \frac{d}{dt} \theta_g(t) = -\rho \frac{d}{dt} V_g(t) - h A_w (\theta_g(t) - \theta_g(t))$

-Mass balance (=volume for incompressible fluid)

 $\frac{d}{dt}V_g(t)=Q_2(t)$

-Ideal gas law

 $p_g(t) = \frac{m_g R_g \theta_g(t)}{V_g(t)}$



Power generation

 $P_2(t) = p_2(t) Q_2(t)$

3

Model Simplification

Simplifications made in thermodynamic equations to get a simple state equation.

Assuming steady state conditions. —Eliminating θ_g and the volume change gives

$$p_2(t) = \frac{h A_w \theta_w m_g R_g}{V_g(t) h A_w + m_g R_g Q_2(t)}$$

► Combining this with the power output gives

$$Q_2(t) = \frac{V_g(t)}{m_g} \frac{h A_w P_2(t)}{R_g \theta_w h A_w - R_g P_2(t)}$$

- ▶ Integrating $Q_2(t)$ gives V_g as the state in the model.
- ▶ Modeling of the hydraulic systems efficiency, see the book.
- A detail for the assignment
 This simplification can give problems in the simulation if parameter values are off. (Division by zero.)

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/lodeling

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Basics

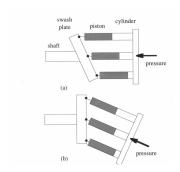
Hydraulic Pumps and Motors

Pneumatic Hybrid Engine Systems

Case studies

35/48

Hydraulic Pumps



Modeling of Hydraulic Motors

► Efficiency modeling

$$\begin{split} P_1(t) = & \frac{P_2(t)}{\eta_{hm}(\omega_2(t), T_2(t))}, & P_2(t) > 0 \\ P_1(t) = & P_2(t) \, \eta_{hm}(\omega_2(t), -|T_2|(t)), & P_2(t) < 0 \end{split}$$

▶ Willans line modeling, describing the loss

$$P_1(t) = \frac{P_2(t) + P_0}{e}$$

 Physical modeling Wilson's approach provided in the book.

37/4

Outline

Repetition

Short Term Storage

Hybrid-Inertial Propulsion Systems

Basic principles

Design princi

Modeling

Continuously Variable Transmission

Hybrid-Hydraulic Propulsion Systems

Basics

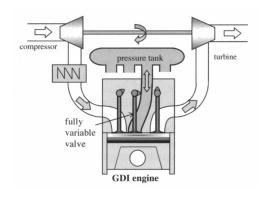
Modeling

Hydraulic Pumps and Motors

Pneumatic Hybrid Engine Systems

Case studies

Pneumatic Hybrid Engine System



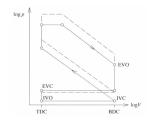
36

Conventional SI Engine

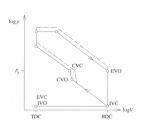
Compression and expansion model

$$p(t) = c v(t)^{-\gamma}$$
 \Rightarrow $\log(p(t)) = \log(c) - \gamma \log(v(t))$

gives lines in the log-log diagram version of the pV-diagram



Super Charged Mode

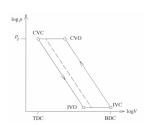


48

Under Charged Mode

P_T CVC EVO CVC EVC CVC DO TDC BDC BDC

Pneumatic Brake System



42/48

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Repetition

Short Term Storage

Hybrid-Inertial Propulsion Systems

Basic principles

Design principles

Modeling

Continuously Variable Transmission

Hybrid-Hydraulic Propulsion Systems

Basics

Modeling

Hydraulic Pumps and Motors

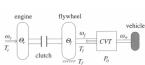
Pneumatic Hybrid Engine Systems

Case studies

Case Study 3: ICE and Flywheel Powertrain

- ► Control of a ICE and Flywheel Powertrain
- ► Switching on and off engine



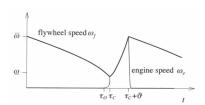


45/48

Problem description

For each constant vehicle speed find the optimal limits for starting and stopping the engine

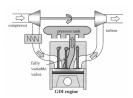
-Minimize fuel consumption



–Solved through parameter optimization \Rightarrow Map used for control

Case Study 8: Hybrid Pneumatic Engine

- ▶ Local optimization of the engine thermodynamic cycle
- ▶ Different modes to select between
- ▶ Dynamic programming of the mode selection



4//48